

Number Link

Ed Pegg Jr

Sudoku is just one of hundreds of great puzzle types. This column presents obscure logic puzzles of various sorts and challenges the readers to solve the puzzles in two ways: by hand and with *Mathematica*. For the latter, solvers are invited to send their code to edp@wolfram.com. The person submitting the most elegant solution will receive a prize.

■ Instructions

During the 1890s, puzzler Sam Loyd wrote columns for the *Brooklyn Daily Eagle*. On February 28, 1897, the following puzzle appeared [1].

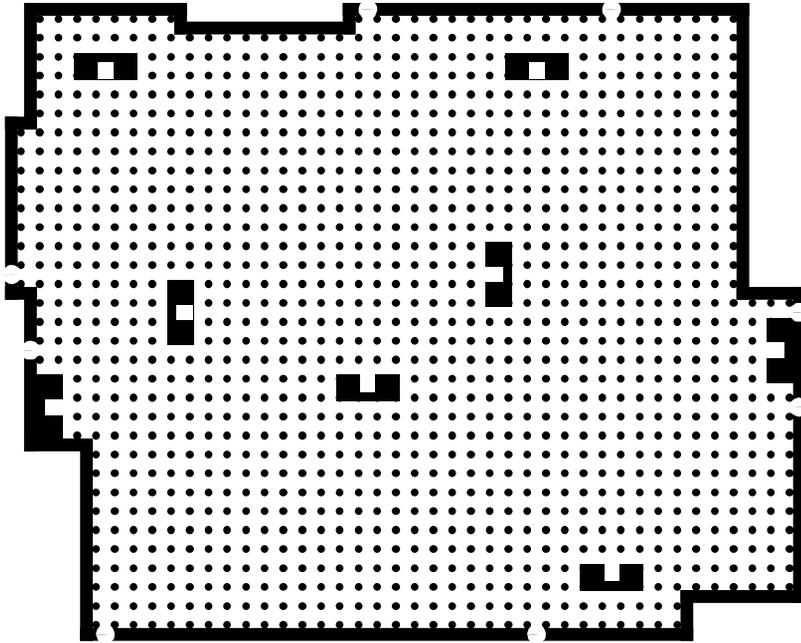
There are eight houses in Puzzleland Park, and the people of each house must only go out of the park by their private gate directly across, on a line with the door of their own house. Each family has a private path of their own leading to their gate between a row of trees; no paths cross any other paths; no inmates of one house ever meet any of their neighbors, so they never quarrel about which should turn out for the other in Puzzleland. Some of the paths are crooked and very funny, but as each one has a map with his particular route marked out by the landlord, who is a great puzzlist, they never get lost. Here is one of the maps, on which you are asked to trace out the paths which each family must take to get to their private gate, across the park, but directly opposite to their door; but remember, none of the paths must cross!

(The solution to this puzzle is on page 6 of the online notebook. The online notebook contains code for the Puzzleland Park layout and code for the layout of the solution.)

This puzzle type is now a regular feature of Japanese puzzle magazines under the name Number Link. The format has been refined in the last hundred years. Each puzzle follows these rules.

1. Connect identical numbers with a continuous path.
2. Paths must go through the center of a cell horizontally or vertically and never go through the same cell twice.
3. Paths cannot cross, branch off, or go through other numbered cells.
4. Every unnumbered square must contain part of a path.

```
In[10]:= Show[PuzzlelandPark]
```

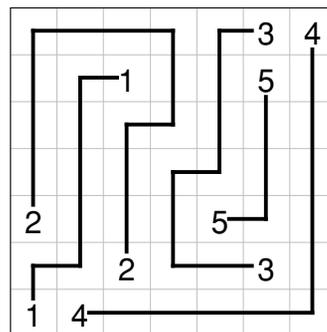


■ Example

Here is an example of a Number Link puzzle and its solution.

```
In[11]:= GraphicsArray[{Numberlink[7, NumberLinkPuz05], Puz05Sol},
  Frame → False, GraphicsSpacing → .05] // Show
```

| | | | | | |
|---|---|---|--|---|---|
| | | | | 3 | 4 |
| | | 1 | | 5 | |
| | | | | | |
| 2 | | | | 5 | |
| | | 2 | | 3 | |
| 1 | 4 | | | | |



■ Puzzle Source

```

In[13]:= NumberLinkPuz01 = {{10, 11}, {17, 21}, {1, 78}, {9, 37}};
In[14]:= NumberLinkPuz02 =
  {{85, 89}, {19, 73}, {18, 83}, {12, 82}, {24, 84}, {37, 52}};
In[15]:= NumberLinkPuz03 =
  {{12, 88}, {23, 96}, {35, 85}, {39, 73}, {36, 89}, {19, 44}};
In[16]:= NumberLinkPuz04 =
  {{4, 91}, {63, 100}, {68, 83}, {12, 77}, {15, 78}, {14, 28}};
In[17]:= NumberLinkPuz05 = {{1, 38}, {10, 15}, {13, 48}, {2, 49}, {19, 41}};

```

■ Previous Issue's Solution

The 10:2 column discussed Ripple Effect puzzles. Yves Papegay sent a complete solution, which is available in `ripple.nb`. His solution qualifies him for *The Mathematica Guidebook* of his choice.

Yves' solution has two parts. First, he checks each cell of each room for the main criteria: only once, not too close, and at least once. These three criteria form what he calls a *Naive* filter. Surprisingly, multiple uses of the *Naive* filter will solve most of the Ripple Effect puzzles given in the previous column. For the remainder, he introduces code to fix all possible values in each cell with a *One Step Further* filter. Fixed values that then fail to give solutions with the *Naive* filter are then discarded as impossible.

■ Additional Material

`ripple.nb`

Available at www.mathematica-journal.com/issue/v10i3/download.

■ References

- [1] S. Loyd, *Sam Loyd's Cyclopedia of 5000 Puzzles, Tricks, and Conundrums (With Answers)*, New York: The Lamb Publishing Company, 1914, p. 61.
www.mathpuzzle.com/loyd/cop060-061.html.
- [2] *Penpa Mix #2*, Tokyo, Japan: NIKOLI Co., Ltd., 2005, pp. 36–37.
www.nikoli.co.jp/howtoget-e.htm.

Ed Pegg Jr
 Scientific Information Editor
 Wolfram Research, Inc.
edp@wolfram.com

■ Puzzleland Park Solution

```
In[18]:= Show[PuzzlelandParkSolution]
```

